

APPENDIX 7*

STATISTICAL METHODOLOGY



ProUCL 95% UCL Soil
East Mountain Assessment Area

Antimony

General Statistics

Number of Valid Observations 36 Number of Distinct Observations 35

Raw Statistics

| | | | |
|--------------------------|-------|---------------------|--------|
| Minimum | 0.211 | Minimum of Log Data | -1.556 |
| Maximum | 137 | Maximum of Log Data | 4.92 |
| Mean | 11.36 | Mean of log Data | 1.493 |
| Median | 5.475 | SD of log Data | 1.454 |
| SD | 23.14 | | |
| Std. Error of Mean | 3.856 | | |
| Coefficient of Variation | 2.036 | | |
| Skewness | 4.873 | | |

Log-transformed Statistics

Relevant UCL Statistics

| | | | |
|--|-------|--|-------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Shapiro Wilk Test Statistic | 0.441 | Shapiro Wilk Test Statistic | 0.962 |
| Shapiro Wilk Critical Value | 0.935 | Shapiro Wilk Critical Value | 0.935 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|----------------------------|-------|
| 95% Student's-t UCL | 17.88 | 95% H-UCL | 26.4 |
| 95% UCLs (Adjusted for Skewness) | | 95% Chebyshev (MVUE) UCL | 28.42 |
| 95% Adjusted-CLT UCL (Chen-1995) | 21.05 | 97.5% Chebyshev (MVUE) UCL | 35.48 |
| 95% Modified-t UCL (Johnson-1978) | 18.4 | 99% Chebyshev (MVUE) UCL | 49.35 |

Assuming Lognormal Distribution

Gamma Distribution Test

| | | | |
|---|--------|---|-------|
| k star (bias corrected) | 0.616 | Data Follow Appr. Gamma Distribution at 5% Significance Level | |
| Theta Star | 18.46 | | |
| MLE of Mean | 11.36 | | |
| MLE of Standard Deviation | 14.48 | | |
| nu star | 44.33 | | |
| Approximate Chi Square Value (.05) | 30.06 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0428 | 95% CLT UCL | 17.71 |
| Adjusted Chi Square Value | 29.52 | 95% Jackknife UCL | 17.88 |
| | | 95% Standard Bootstrap UCL | 17.58 |
| Anderson-Darling Test Statistic | 0.836 | 95% Bootstrap-t UCL | 30.11 |
| Anderson-Darling 5% Critical Value | 0.798 | 95% Hall's Bootstrap UCL | 41.23 |
| Kolmogorov-Smirnov Test Statistic | 0.14 | 95% Percentile Bootstrap UCL | 18.55 |
| Kolmogorov-Smirnov 5% Critical Value | 0.154 | 95% BCA Bootstrap UCL | 22.22 |
| Data follow Appr. Gamma Distribution at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 28.17 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 35.45 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 49.73 |
| 95% Approximate Gamma UCL | 16.76 | | |
| 95% Adjusted Gamma UCL | 17.06 | | |

Data Distribution

Potential UCL to Use Use 95% Approximate Gamma UCL 16.76

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Arsenic

General Statistics

Number of Valid Observations 43 Number of Distinct Observations 43

Raw Statistics

| | | |
|--------------------------|----------------------------|-------|
| | Log-transformed Statistics | |
| Minimum | 4.25 Minimum of Log Data | 1.447 |
| Maximum | 615 Maximum of Log Data | 6.422 |
| Mean | 98.47 Mean of log Data | 4.131 |
| Median | 63.9 SD of log Data | 1.026 |
| SD | 108.5 | |
| Std. Error of Mean | 16.54 | |
| Coefficient of Variation | 1.101 | |
| Skewness | 2.986 | |

Relevant UCL Statistics

| | | |
|--|--|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.709 Shapiro Wilk Test Statistic | 0.967 |
| Shapiro Wilk Critical Value | 0.943 Shapiro Wilk Critical Value | 0.943 |
| Data not Normal at 5% Significance Level | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|----------------------------------|-------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 126.3 95% H-UCL | 153.9 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 186.5 |
| 95% Adjusted-CLT UCL (Chen-1995) | 133.7 97.5% Chebyshev (MVUE) UCL | 222.4 |
| 95% Modified-t UCL (Johnson-1978) | 127.5 99% Chebyshev (MVUE) UCL | 293 |

Gamma Distribution Test

| | | |
|--|--|-------|
| | Data Distribution | |
| k star (bias corrected) | 1.159 Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 84.95 | |
| MLE of Mean | 98.47 | |
| MLE of Standard Deviation | 91.46 | |
| nu star | 99.69 | |
| Approximate Chi Square Value (.05) | 77.66 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0444 95% CLT UCL | 125.7 |
| Adjusted Chi Square Value | 76.98 95% Jackknife UCL | 126.3 |
| | 95% Standard Bootstrap UCL | 125.1 |
| Anderson-Darling Test Statistic | 0.539 95% Bootstrap-t UCL | 139.2 |
| Anderson-Darling 5% Critical Value | 0.773 95% Hall's Bootstrap UCL | 172.7 |
| Kolmogorov-Smirnov Test Statistic | 0.112 95% Percentile Bootstrap UCL | 126.6 |
| Kolmogorov-Smirnov 5% Critical Value | 0.138 95% BCA Bootstrap UCL | 133.3 |
| Data appear Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 170.6 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 201.8 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 263 |
| 95% Approximate Gamma UCL | 126.4 | |
| 95% Adjusted Gamma UCL | 127.5 | |

Potential UCL to Use Use 95% Approximate Gamma UCL 126.4

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Cadmium

General Statistics

Number of Valid Observations 43 Number of Distinct Observations 38

Raw Statistics

| | | |
|--------------------------|----------------------------|--------|
| | Log-transformed Statistics | |
| Minimum | 0.0431 Minimum of Log Data | -3.144 |
| Maximum | 132 Maximum of Log Data | 4.883 |
| Mean | 24.43 Mean of log Data | 2.505 |
| Median | 14.6 SD of log Data | 1.492 |
| SD | 29.06 | |
| Std. Error of Mean | 4.431 | |
| Coefficient of Variation | 1.19 | |
| Skewness | 2.363 | |

Relevant UCL Statistics

| | | |
|--|---|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.71 Shapiro Wilk Test Statistic | 0.882 |
| Shapiro Wilk Critical Value | 0.943 Shapiro Wilk Critical Value | 0.943 |
| Data not Normal at 5% Significance Level | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|----------------------------------|-------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 31.88 95% H-UCL | 73.71 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 81.34 |
| 95% Adjusted-CLT UCL (Chen-1995) | 33.42 97.5% Chebyshev (MVUE) UCL | 101.2 |
| 95% Modified-t UCL (Johnson-1978) | 32.14 99% Chebyshev (MVUE) UCL | 140.3 |

Gamma Distribution Test

| | | |
|--|--|-------|
| | Data Distribution | |
| k star (bias corrected) | 0.808 Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 30.22 | |
| MLE of Mean | 24.43 | |
| MLE of Standard Deviation | 27.17 | |
| nu star | 69.5 | |
| Approximate Chi Square Value (.05) | 51.31 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0444 95% CLT UCL | 31.71 |
| Adjusted Chi Square Value | 50.77 95% Jackknife UCL | 31.88 |
| | 95% Standard Bootstrap UCL | 31.59 |
| Anderson-Darling Test Statistic | 0.597 95% Bootstrap-t UCL | 35.53 |
| Anderson-Darling 5% Critical Value | 0.785 95% Hall's Bootstrap UCL | 34.23 |
| Kolmogorov-Smirnov Test Statistic | 0.113 95% Percentile Bootstrap UCL | 31.81 |
| Kolmogorov-Smirnov 5% Critical Value | 0.14 95% BCA Bootstrap UCL | 33.97 |
| Data appear Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 43.74 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 52.1 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 68.52 |
| 95% Approximate Gamma UCL | 33.08 | |
| 95% Adjusted Gamma UCL | 33.44 | |

Potential UCL to Use Use 95% Approximate Gamma UCL 33.08

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Copper

General Statistics

Number of Valid Observations 43 Number of Distinct Observations 41

Raw Statistics

| | | |
|--------------------------|----------------------------|-------|
| | Log-transformed Statistics | |
| Minimum | 2.83 Minimum of Log Data | 1.04 |
| Maximum | 5460 Maximum of Log Data | 8.605 |
| Mean | 818.7 Mean of log Data | 5.666 |
| Median | 393 SD of log Data | 1.802 |
| SD | 1111 | |
| Std. Error of Mean | 169.4 | |
| Coefficient of Variation | 1.357 | |
| Skewness | 2.485 | |

Relevant UCL Statistics

| | | |
|--|---|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.715 Shapiro Wilk Test Statistic | 0.942 |
| Shapiro Wilk Critical Value | 0.943 Shapiro Wilk Critical Value | 0.943 |
| Data not Normal at 5% Significance Level | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|---------------------------------|------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 1104 95% H-UCL | 3757 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 3563 |
| 95% Adjusted-CLT UCL (Chen-1995) | 1166 97.5% Chebyshev (MVUE) UCL | 4526 |
| 95% Modified-t UCL (Johnson-1978) | 1114 99% Chebyshev (MVUE) UCL | 6416 |

Gamma Distribution Test

| | | |
|--|--|------|
| | Data Distribution | |
| k star (bias corrected) | 0.568 Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 1441 | |
| MLE of Mean | 818.7 | |
| MLE of Standard Deviation | 1086 | |
| nu star | 48.86 | |
| Approximate Chi Square Value (.05) | 33.81 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0444 95% CLT UCL | 1097 |
| Adjusted Chi Square Value | 33.38 95% Jackknife UCL | 1104 |
| | 95% Standard Bootstrap UCL | 1090 |
| Anderson-Darling Test Statistic | 0.242 95% Bootstrap-t UCL | 1197 |
| Anderson-Darling 5% Critical Value | 0.804 95% Hall's Bootstrap UCL | 1236 |
| Kolmogorov-Smirnov Test Statistic | 0.0931 95% Percentile Bootstrap UCL | 1110 |
| Kolmogorov-Smirnov 5% Critical Value | 0.142 95% BCA Bootstrap UCL | 1186 |
| Data appear Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 1557 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 1876 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 2504 |
| 95% Approximate Gamma UCL | 1183 | |
| 95% Adjusted Gamma UCL | 1198 | |

Potential UCL to Use Use 95% Approximate Gamma UCL 1183

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Lead

General Statistics

Number of Valid Observations 43 Number of Distinct Observations 43

Raw Statistics

| | | |
|--------------------------|----------------------------|-------|
| | Log-transformed Statistics | |
| Minimum | 2.51 Minimum of Log Data | 0.92 |
| Maximum | 5570 Maximum of Log Data | 8.625 |
| Mean | 736.5 Mean of log Data | 5.66 |
| Median | 400 SD of log Data | 1.723 |
| SD | 981.2 | |
| Std. Error of Mean | 149.6 | |
| Coefficient of Variation | 1.332 | |
| Skewness | 3.15 | |

Relevant UCL Statistics

| | | |
|--|---|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.694 Shapiro Wilk Test Statistic | 0.938 |
| Shapiro Wilk Critical Value | 0.943 Shapiro Wilk Critical Value | 0.943 |
| Data not Normal at 5% Significance Level | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|---------------------------------|------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 988.2 95% H-UCL | 3021 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 3002 |
| 95% Adjusted-CLT UCL (Chen-1995) | 1059 97.5% Chebyshev (MVUE) UCL | 3794 |
| 95% Modified-t UCL (Johnson-1978) | 1000 99% Chebyshev (MVUE) UCL | 5351 |

Gamma Distribution Test

| | | |
|--|--|-------|
| | Data Distribution | |
| k star (bias corrected) | 0.619 Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 1191 | |
| MLE of Mean | 736.5 | |
| MLE of Standard Deviation | 936.4 | |
| nu star | 53.21 | |
| Approximate Chi Square Value (.05) | 37.45 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0444 95% CLT UCL | 982.7 |
| Adjusted Chi Square Value | 36.99 95% Jackknife UCL | 988.2 |
| | 95% Standard Bootstrap UCL | 978 |
| Anderson-Darling Test Statistic | 0.193 95% Bootstrap-t UCL | 1123 |
| Anderson-Darling 5% Critical Value | 0.799 95% Hall's Bootstrap UCL | 2013 |
| Kolmogorov-Smirnov Test Statistic | 0.0624 95% Percentile Bootstrap UCL | 990.2 |
| Kolmogorov-Smirnov 5% Critical Value | 0.141 95% BCA Bootstrap UCL | 1079 |
| Data appear Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 1389 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 1671 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 2225 |
| 95% Approximate Gamma UCL | 1046 | |
| 95% Adjusted Gamma UCL | 1059 | |

Potential UCL to Use Use 95% Approximate Gamma UCL 1046

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Mercury

General Statistics

Number of Valid Observations 36 Number of Distinct Observations 36

Raw Statistics

| | | |
|--------------------------|----------------------------|--------|
| | Log-transformed Statistics | |
| Minimum | 0.0141 Minimum of Log Data | -4.262 |
| Maximum | 1.82 Maximum of Log Data | 0.599 |
| Mean | 0.373 Mean of log Data | -1.72 |
| Median | 0.144 SD of log Data | 1.317 |
| SD | 0.445 | |
| Std. Error of Mean | 0.0741 | |
| Coefficient of Variation | 1.193 | |
| Skewness | 1.634 | |

Relevant UCL Statistics

| | | |
|--|--|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.768 Shapiro Wilk Test Statistic | 0.958 |
| Shapiro Wilk Critical Value | 0.935 Shapiro Wilk Critical Value | 0.935 |
| Data not Normal at 5% Significance Level | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|----------------------------------|-------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 0.498 95% H-UCL | 0.789 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 0.895 |
| 95% Adjusted-CLT UCL (Chen-1995) | 0.516 97.5% Chebyshev (MVUE) UCL | 1.105 |
| 95% Modified-t UCL (Johnson-1978) | 0.502 99% Chebyshev (MVUE) UCL | 1.518 |

Gamma Distribution Test

| | | |
|---|--|-------|
| | Data Distribution | |
| k star (bias corrected) | 0.759 Data appear Lognormal at 5% Significance Level | |
| Theta Star | 0.491 | |
| MLE of Mean | 0.373 | |
| MLE of Standard Deviation | 0.428 | |
| nu star | 54.68 | |
| Approximate Chi Square Value (.05) | 38.69 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0428 95% CLT UCL | 0.495 |
| Adjusted Chi Square Value | 38.08 95% Jackknife UCL | 0.498 |
| | 95% Standard Bootstrap UCL | 0.494 |
| Anderson-Darling Test Statistic | 0.804 95% Bootstrap-t UCL | 0.537 |
| Anderson-Darling 5% Critical Value | 0.785 95% Hall's Bootstrap UCL | 0.526 |
| Kolmogorov-Smirnov Test Statistic | 0.161 95% Percentile Bootstrap UCL | 0.497 |
| Kolmogorov-Smirnov 5% Critical Value | 0.152 95% BCA Bootstrap UCL | 0.509 |
| Data not Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 0.696 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 0.836 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 1.11 |
| 95% Approximate Gamma UCL | 0.527 | |
| 95% Adjusted Gamma UCL | 0.536 | |

Potential UCL to Use Use 95% H-UCL 0.789

ProUCL computes and outputs H-statistic based UCLs for historical reasons only. H-statistic often results in unstable (both high and low) values of UCL95 as shown in examples in the Technical Guide. It is therefore recommended to avoid the use of H-statistic based 95% UCLs. Use of nonparametric methods are preferred to compute UCL95 for skewed data sets which do not follow a gamma distribution.

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Selenium

General Statistics

| | | | |
|------------------------------|----|---------------------------------|----|
| Number of Valid Observations | 36 | Number of Distinct Observations | 36 |
|------------------------------|----|---------------------------------|----|

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.156 | Minimum of Log Data | -1.858 |
| Maximum | 16.3 | Maximum of Log Data | 2.791 |
| Mean | 2.178 | Mean of log Data | 0.215 |
| Median | 1.43 | SD of log Data | 1.106 |
| SD | 2.884 | | |
| Std. Error of Mean | 0.481 | | |
| Coefficient of Variation | 1.324 | | |
| Skewness | 3.682 | | |

Relevant UCL Statistics

| | | | |
|--|-------|--|-------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Shapiro Wilk Test Statistic | 0.617 | Shapiro Wilk Test Statistic | 0.972 |
| Shapiro Wilk Critical Value | 0.935 | Shapiro Wilk Critical Value | 0.935 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| | | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 2.99 | 95% H-UCL | 3.653 |
| 95% UCLs (Adjusted for Skewness) | | 95% Chebyshev (MVUE) UCL | 4.353 |
| 95% Adjusted-CLT UCL (Chen-1995) | 3.284 | 97.5% Chebyshev (MVUE) UCL | 5.273 |
| 95% Modified-t UCL (Johnson-1978) | 3.04 | 99% Chebyshev (MVUE) UCL | 7.08 |

Gamma Distribution Test

| | | | |
|--|--------|--|-------|
| | | Data Distribution | |
| k star (bias corrected) | 0.955 | Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 2.281 | | |
| MLE of Mean | 2.178 | | |
| MLE of Standard Deviation | 2.229 | | |
| nu star | 68.75 | | |
| Approximate Chi Square Value (.05) | 50.67 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0428 | 95% CLT UCL | 2.969 |
| Adjusted Chi Square Value | 49.96 | 95% Jackknife UCL | 2.99 |
| | | 95% Standard Bootstrap UCL | 2.961 |
| Anderson-Darling Test Statistic | 0.422 | 95% Bootstrap-t UCL | 3.706 |
| Anderson-Darling 5% Critical Value | 0.776 | 95% Hall's Bootstrap UCL | 6.669 |
| Kolmogorov-Smirnov Test Statistic | 0.0899 | 95% Percentile Bootstrap UCL | 3.047 |
| Kolmogorov-Smirnov 5% Critical Value | 0.151 | 95% BCA Bootstrap UCL | 3.328 |
| Data appear Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 4.274 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 5.18 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 6.961 |
| 95% Approximate Gamma UCL | 2.956 | | |
| 95% Adjusted Gamma UCL | 2.997 | | |

| | | | |
|----------------------|--|-------------------------------|-------|
| Potential UCL to Use | | Use 95% Approximate Gamma UCL | 2.956 |
|----------------------|--|-------------------------------|-------|

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Silver

General Statistics

Number of Valid Observations 36 Number of Distinct Observations 36

Raw Statistics

| | | |
|--------------------------|----------------------------|--------|
| | Log-transformed Statistics | |
| Minimum | 0.0867 Minimum of Log Data | -2.445 |
| Maximum | 44.5 Maximum of Log Data | 3.795 |
| Mean | 4.448 Mean of log Data | 0.465 |
| Median | 2.065 SD of log Data | 1.592 |
| SD | 7.88 | |
| Std. Error of Mean | 1.313 | |
| Coefficient of Variation | 1.772 | |
| Skewness | 4.056 | |

Relevant UCL Statistics

| | | |
|--|--|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.542 Shapiro Wilk Test Statistic | 0.955 |
| Shapiro Wilk Critical Value | 0.935 Shapiro Wilk Critical Value | 0.935 |
| Data not Normal at 5% Significance Level | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|----------------------------------|-------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 6.667 95% H-UCL | 13.12 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 13.2 |
| 95% Adjusted-CLT UCL (Chen-1995) | 7.557 97.5% Chebyshev (MVUE) UCL | 16.64 |
| 95% Modified-t UCL (Johnson-1978) | 6.815 99% Chebyshev (MVUE) UCL | 23.39 |

Gamma Distribution Test

| | | |
|--|--|-------|
| | Data Distribution | |
| k star (bias corrected) | 0.569 Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 7.813 | |
| MLE of Mean | 4.448 | |
| MLE of Standard Deviation | 5.895 | |
| nu star | 40.99 | |
| Approximate Chi Square Value (.05) | 27.32 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0428 95% CLT UCL | 6.609 |
| Adjusted Chi Square Value | 26.81 95% Jackknife UCL | 6.667 |
| | 95% Standard Bootstrap UCL | 6.571 |
| Anderson-Darling Test Statistic | 0.6 95% Bootstrap-t UCL | 8.954 |
| Anderson-Darling 5% Critical Value | 0.803 95% Hall's Bootstrap UCL | 14.94 |
| Kolmogorov-Smirnov Test Statistic | 0.141 95% Percentile Bootstrap UCL | 6.596 |
| Kolmogorov-Smirnov 5% Critical Value | 0.154 95% BCA Bootstrap UCL | 8.071 |
| Data appear Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 10.17 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 12.65 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 17.52 |
| 95% Approximate Gamma UCL | 6.674 | |
| 95% Adjusted Gamma UCL | 6.801 | |

Potential UCL to Use Use 95% Approximate Gamma UCL 6.674

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Zinc

General Statistics

Number of Valid Observations 43 Number of Distinct Observations 43

Raw Statistics

| | | |
|--------------------------|----------------------------|-------|
| | Log-transformed Statistics | |
| Minimum | 10 Minimum of Log Data | 2.303 |
| Maximum | 3270 Maximum of Log Data | 8.093 |
| Mean | 541 Mean of log Data | 5.523 |
| Median | 312 SD of log Data | 1.384 |
| SD | 689.4 | |
| Std. Error of Mean | 105.1 | |
| Coefficient of Variation | 1.274 | |
| Skewness | 2.222 | |

Relevant UCL Statistics

| | | |
|--|--|-------|
| | Lognormal Distribution Test | |
| Normal Distribution Test | | |
| Shapiro Wilk Test Statistic | 0.724 Shapiro Wilk Test Statistic | 0.973 |
| Shapiro Wilk Critical Value | 0.943 Shapiro Wilk Critical Value | 0.943 |
| Data not Normal at 5% Significance Level | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | |
|-----------------------------------|---------------------------------|------|
| | Assuming Lognormal Distribution | |
| 95% Student's-t UCL | 717.9 95% H-UCL | 1192 |
| 95% UCLs (Adjusted for Skewness) | 95% Chebyshev (MVUE) UCL | 1363 |
| 95% Adjusted-CLT UCL (Chen-1995) | 752 97.5% Chebyshev (MVUE) UCL | 1681 |
| 95% Modified-t UCL (Johnson-1978) | 723.8 99% Chebyshev (MVUE) UCL | 2307 |

Gamma Distribution Test

| | | |
|--|--|-------|
| | Data Distribution | |
| k star (bias corrected) | 0.736 Data appear Gamma Distributed at 5% Significance Level | |
| Theta Star | 735.5 | |
| MLE of Mean | 541 | |
| MLE of Standard Deviation | 630.8 | |
| nu star | 63.26 | |
| Approximate Chi Square Value (.05) | 45.96 Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0444 95% CLT UCL | 714 |
| Adjusted Chi Square Value | 45.45 95% Jackknife UCL | 717.9 |
| | 95% Standard Bootstrap UCL | 710.8 |
| Anderson-Darling Test Statistic | 0.501 95% Bootstrap-t UCL | 774.2 |
| Anderson-Darling 5% Critical Value | 0.788 95% Hall's Bootstrap UCL | 781.8 |
| Kolmogorov-Smirnov Test Statistic | 0.115 95% Percentile Bootstrap UCL | 709.7 |
| Kolmogorov-Smirnov 5% Critical Value | 0.14 95% BCA Bootstrap UCL | 783.5 |
| Data appear Gamma Distributed at 5% Significance Level | 95% Chebyshev(Mean, Sd) UCL | 999.3 |
| | 97.5% Chebyshev(Mean, Sd) UCL | 1198 |
| Assuming Gamma Distribution | 99% Chebyshev(Mean, Sd) UCL | 1587 |
| 95% Approximate Gamma UCL | 744.6 | |
| 95% Adjusted Gamma UCL | 753 | |

Potential UCL to Use Use 95% Approximate Gamma UCL 744.6

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Chromium

General Statistics

Number of Valid Observations 45 Number of Distinct Observations 42

Raw Statistics

| | | | |
|--------------------------|-------|---------------------|--------|
| Minimum | 0.4 | Minimum of Log Data | -0.916 |
| Maximum | 130 | Maximum of Log Data | 4.868 |
| Mean | 18.75 | Mean of log Data | 1.893 |
| Median | 4.66 | SD of log Data | 1.341 |
| SD | 32.13 | | |
| Std. Error of Mean | 4.79 | | |
| Coefficient of Variation | 1.714 | | |
| Skewness | 2.088 | | |

Log-transformed Statistics

Relevant UCL Statistics

| | | | |
|--|-------|---|-------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Shapiro Wilk Test Statistic | 0.563 | Shapiro Wilk Test Statistic | 0.888 |
| Shapiro Wilk Critical Value | 0.945 | Shapiro Wilk Critical Value | 0.945 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|----------------------------|-------|
| 95% Student's-t UCL | 26.79 | 95% H-UCL | 28.64 |
| 95% UCLs (Adjusted for Skewness) | | 95% Chebyshev (MVUE) UCL | 33.17 |
| 95% Adjusted-CLT UCL (Chen-1995) | 28.22 | 97.5% Chebyshev (MVUE) UCL | 40.71 |
| 95% Modified-t UCL (Johnson-1978) | 27.04 | 99% Chebyshev (MVUE) UCL | 55.52 |

Assuming Lognormal Distribution

Gamma Distribution Test

| | | | |
|---|--------|-------------------------------|--|
| k star (bias corrected) | 0.571 | Data Distribution | Data do not follow a Discernable Distribution (0.05) |
| Theta Star | 32.84 | | |
| MLE of Mean | 18.75 | | |
| MLE of Standard Deviation | 24.81 | | |
| nu star | 51.38 | | |
| Approximate Chi Square Value (.05) | 35.91 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0447 | 95% CLT UCL | 26.62 |
| Adjusted Chi Square Value | 35.49 | 95% Jackknife UCL | 26.79 |
| | | 95% Standard Bootstrap UCL | 26.61 |
| Anderson-Darling Test Statistic | 4.797 | 95% Bootstrap-t UCL | 28.89 |
| Anderson-Darling 5% Critical Value | 0.804 | 95% Hall's Bootstrap UCL | 27.34 |
| Kolmogorov-Smirnov Test Statistic | 0.297 | 95% Percentile Bootstrap UCL | 26.98 |
| Kolmogorov-Smirnov 5% Critical Value | 0.138 | 95% BCA Bootstrap UCL | 29.16 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 39.62 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 48.66 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 66.41 |
| 95% Approximate Gamma UCL | 26.82 | | |
| 95% Adjusted Gamma UCL | 27.14 | | |

Potential UCL to Use Use 95% Chebyshev (Mean, Sd) UCL 39.62

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

ProUCL 95% UCL Soil
South Arroyo Open Space

Antimony

General Statistics

| | | | |
|------------------------------|-----|---------------------------------|-----|
| Number of Valid Observations | 159 | Number of Distinct Observations | 129 |
| Number of Missing Values | 23 | | |

Raw Statistics

| | | | |
|--------------------------|--------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.198 | Minimum of Log Data | -1.619 |
| Maximum | 2.22 | Maximum of Log Data | 0.798 |
| Mean | 0.888 | Mean of log Data | -0.283 |
| Median | 0.741 | SD of log Data | 0.588 |
| SD | 0.497 | | |
| Std. Error of Mean | 0.0394 | | |
| Coefficient of Variation | 0.56 | | |
| Skewness | 0.713 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.15 | Lilliefors Test Statistic | 0.109 |
| Lilliefors Critical Value | 0.0703 | Lilliefors Critical Value | 0.0703 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 0.953 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 0.979 |
| 95% Adjusted-CLT UCL (Chen-1995) | 0.955 | 95% Chebyshev (MVUE) UCL | 1.091 |
| 95% Modified-t UCL (Johnson-1978) | 0.953 | 97.5% Chebyshev (MVUE) UCL | 1.176 |
| | | 99% Chebyshev (MVUE) UCL | 1.343 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 3.161 | Data Distribution | |
| Theta Star | 0.281 | Data do not follow a Discernable Distribution (0.05) | |
| MLE of Mean | 0.888 | | |
| MLE of Standard Deviation | 0.499 | | |
| nu star | 1005 | | |
| Approximate Chi Square Value (.05) | 932.7 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0485 | 95% CLT UCL | 0.952 |
| Adjusted Chi Square Value | 932.1 | 95% Jackknife UCL | 0.953 |
| | | 95% Standard Bootstrap UCL | 0.949 |
| Anderson-Darling Test Statistic | 2.037 | 95% Bootstrap-t UCL | 0.954 |
| Anderson-Darling 5% Critical Value | 0.759 | 95% Hall's Bootstrap UCL | 0.955 |
| Kolmogorov-Smirnov Test Statistic | 0.128 | 95% Percentile Bootstrap UCL | 0.953 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0747 | 95% BCA Bootstrap UCL | 0.955 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 1.059 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 1.134 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 1.28 |
| 95% Approximate Gamma UCL | 0.957 | | |
| 95% Adjusted Gamma UCL | 0.957 | | |

Potential UCL to Use

| | |
|----------------------------------|-------|
| Use 95% Chebyshev (Mean, Sd) UCL | 1.059 |
|----------------------------------|-------|

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Arsenic

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 156

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|-------|
| | | Log-transformed Statistics | |
| Minimum | 2.48 | Minimum of Log Data | 0.908 |
| Maximum | 82.6 | Maximum of Log Data | 4.414 |
| Mean | 19.58 | Mean of log Data | 2.735 |
| Median | 15.65 | SD of log Data | 0.693 |
| SD | 14.76 | | |
| Std. Error of Mean | 1.094 | | |
| Coefficient of Variation | 0.754 | | |
| Skewness | 1.823 | | |

Relevant UCL Statistics

| | | | |
|--|--------|--|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.15 | Lilliefors Test Statistic | 0.038 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 21.39 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 21.65 |
| 95% Adjusted-CLT UCL (Chen-1995) | 21.54 | 95% Chebyshev (MVUE) UCL | 24.42 |
| 95% Modified-t UCL (Johnson-1978) | 21.42 | 97.5% Chebyshev (MVUE) UCL | 26.52 |
| | | 99% Chebyshev (MVUE) UCL | 30.64 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 2.204 | Data Distribution | |
| Theta Star | 8.885 | Data appear Lognormal at 5% Significance Level | |
| MLE of Mean | 19.58 | | |
| MLE of Standard Deviation | 13.19 | | |
| nu star | 802.3 | | |
| Approximate Chi Square Value (.05) | 737.6 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 21.38 |
| Adjusted Chi Square Value | 737.1 | 95% Jackknife UCL | 21.39 |
| | | 95% Standard Bootstrap UCL | 21.39 |
| Anderson-Darling Test Statistic | 1.521 | 95% Bootstrap-t UCL | 21.6 |
| Anderson-Darling 5% Critical Value | 0.765 | 95% Hall's Bootstrap UCL | 21.67 |
| Kolmogorov-Smirnov Test Statistic | 0.0692 | 95% Percentile Bootstrap UCL | 21.4 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0691 | 95% BCA Bootstrap UCL | 21.45 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 24.35 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 26.42 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 30.47 |
| 95% Approximate Gamma UCL | 21.3 | | |
| 95% Adjusted Gamma UCL | 21.32 | | |

Potential UCL to Use Use 95% H-UCL 21.65

ProUCL computes and outputs H-statistic based UCLs for historical reasons only. H-statistic often results in unstable (both high and low) values of UCL95 as shown in examples in the Technical Guide. It is therefore recommended to avoid the use of H-statistic based 95% UCLs. Use of nonparametric methods are preferred to compute UCL95 for skewed data sets which do not follow a gamma distribution.

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Barium

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 147

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|-------|
| | | Log-transformed Statistics | |
| Minimum | 24.7 | Minimum of Log Data | 3.207 |
| Maximum | 530 | Maximum of Log Data | 6.273 |
| Mean | 123.4 | Mean of log Data | 4.695 |
| Median | 108 | SD of log Data | 0.47 |
| SD | 71.87 | | |
| Std. Error of Mean | 5.327 | | |
| Coefficient of Variation | 0.583 | | |
| Skewness | 2.642 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.183 | Lilliefors Test Statistic | 0.0747 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 132.2 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 130.1 |
| 95% Adjusted-CLT UCL (Chen-1995) | 133.3 | 95% Chebyshev (MVUE) UCL | 141.5 |
| 95% Modified-t UCL (Johnson-1978) | 132.4 | 97.5% Chebyshev (MVUE) UCL | 150 |
| | | 99% Chebyshev (MVUE) UCL | 166.5 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 4.253 | Data Distribution | |
| Theta Star | 29.01 | Data do not follow a Discernable Distribution (0.05) | |
| MLE of Mean | 123.4 | | |
| MLE of Standard Deviation | 59.83 | | |
| nu star | 1548 | | |
| Approximate Chi Square Value (.05) | 1458 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 132.1 |
| Adjusted Chi Square Value | 1457 | 95% Jackknife UCL | 132.2 |
| | | 95% Standard Bootstrap UCL | 132.1 |
| Anderson-Darling Test Statistic | 2.915 | 95% Bootstrap-t UCL | 133.2 |
| Anderson-Darling 5% Critical Value | 0.756 | 95% Hall's Bootstrap UCL | 133.8 |
| Kolmogorov-Smirnov Test Statistic | 0.111 | 95% Percentile Bootstrap UCL | 132.5 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0685 | 95% BCA Bootstrap UCL | 133.5 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 146.6 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 156.6 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 176.4 |
| 95% Approximate Gamma UCL | 131 | | |
| 95% Adjusted Gamma UCL | 131.1 | | |

Potential UCL to Use

| | |
|-------------------------|-------|
| Use 95% Student's-t UCL | 132.2 |
| or 95% Modified-t UCL | 132.4 |

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Cadmium

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 168

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.101 | Minimum of Log Data | -2.293 |
| Maximum | 27.2 | Maximum of Log Data | 3.303 |
| Mean | 4.534 | Mean of log Data | 0.934 |
| Median | 2.935 | SD of log Data | 1.165 |
| SD | 5.028 | | |
| Std. Error of Mean | 0.373 | | |
| Coefficient of Variation | 1.109 | | |
| Skewness | 2.151 | | |

Relevant UCL Statistics

| | | | |
|--|--------|--|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.189 | Lilliefors Test Statistic | 0.0621 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 5.151 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 6.129 |
| 95% Adjusted-CLT UCL (Chen-1995) | 5.211 | 95% Chebyshev (MVUE) UCL | 7.374 |
| 95% Modified-t UCL (Johnson-1978) | 5.16 | 97.5% Chebyshev (MVUE) UCL | 8.409 |
| | | 99% Chebyshev (MVUE) UCL | 10.44 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 0.986 | Data Distribution | |
| Theta Star | 4.597 | Data appear Lognormal at 5% Significance Level | |
| MLE of Mean | 4.534 | | |
| MLE of Standard Deviation | 4.566 | | |
| nu star | 359 | | |
| Approximate Chi Square Value (.05) | 316.1 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 5.147 |
| Adjusted Chi Square Value | 315.8 | 95% Jackknife UCL | 5.151 |
| | | 95% Standard Bootstrap UCL | 5.141 |
| Anderson-Darling Test Statistic | 1.057 | 95% Bootstrap-t UCL | 5.22 |
| Anderson-Darling 5% Critical Value | 0.784 | 95% Hall's Bootstrap UCL | 5.247 |
| Kolmogorov-Smirnov Test Statistic | 0.0706 | 95% Percentile Bootstrap UCL | 5.177 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0703 | 95% BCA Bootstrap UCL | 5.191 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 6.159 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 6.862 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 8.243 |
| 95% Approximate Gamma UCL | 5.15 | | |
| 95% Adjusted Gamma UCL | 5.155 | | |

Potential UCL to Use Use 95% H-UCL 6.129

ProUCL computes and outputs H-statistic based UCLs for historical reasons only. H-statistic often results in unstable (both high and low) values of UCL95 as shown in examples in the Technical Guide. It is therefore recommended to avoid the use of H-statistic based 95% UCLs. Use of nonparametric methods are preferred to compute UCL95 for skewed data sets which do not follow a gamma distribution.

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Chromium

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 165

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.736 | Minimum of Log Data | -0.307 |
| Maximum | 41.1 | Maximum of Log Data | 3.716 |
| Mean | 6.345 | Mean of log Data | 1.667 |
| Median | 5.655 | SD of log Data | 0.626 |
| SD | 4.344 | | |
| Std. Error of Mean | 0.322 | | |
| Coefficient of Variation | 0.685 | | |
| Skewness | 3.63 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.14 | Lilliefors Test Statistic | 0.0734 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 6.877 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 7.03 |
| 95% Adjusted-CLT UCL (Chen-1995) | 6.967 | 95% Chebyshev (MVUE) UCL | 7.848 |
| 95% Modified-t UCL (Johnson-1978) | 6.892 | 97.5% Chebyshev (MVUE) UCL | 8.46 |
| | | 99% Chebyshev (MVUE) UCL | 9.664 |

Gamma Distribution Test

| | | | |
|---|--------|---|-------|
| k star (bias corrected) | 2.873 | Data Distribution | |
| Theta Star | 2.208 | Data Follow Appr. Gamma Distribution at 5% Significance Level | |
| MLE of Mean | 6.345 | | |
| MLE of Standard Deviation | 3.743 | | |
| nu star | 1046 | | |
| Approximate Chi Square Value (.05) | 971.8 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 6.874 |
| Adjusted Chi Square Value | 971.2 | 95% Jackknife UCL | 6.877 |
| | | 95% Standard Bootstrap UCL | 6.888 |
| Anderson-Darling Test Statistic | 1.15 | 95% Bootstrap-t UCL | 6.999 |
| Anderson-Darling 5% Critical Value | 0.761 | 95% Hall's Bootstrap UCL | 7.089 |
| Kolmogorov-Smirnov Test Statistic | 0.0578 | 95% Percentile Bootstrap UCL | 6.928 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0688 | 95% BCA Bootstrap UCL | 7.013 |
| Data follow Appr. Gamma Distribution at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 7.748 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 8.355 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 9.548 |
| 95% Approximate Gamma UCL | 6.828 | | |
| 95% Adjusted Gamma UCL | 6.832 | | |

Potential UCL to Use Use 95% Approximate Gamma UCL 6.828

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Cobalt

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 157

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.489 | Minimum of Log Data | -0.715 |
| Maximum | 14.2 | Maximum of Log Data | 2.653 |
| Mean | 4.621 | Mean of log Data | 1.425 |
| Median | 4.455 | SD of log Data | 0.492 |
| SD | 2.077 | | |
| Std. Error of Mean | 0.154 | | |
| Coefficient of Variation | 0.45 | | |
| Skewness | 1.282 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.0807 | Lilliefors Test Statistic | 0.0953 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 4.876 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 5.013 |
| 95% Adjusted-CLT UCL (Chen-1995) | 4.89 | 95% Chebyshev (MVUE) UCL | 5.475 |
| 95% Modified-t UCL (Johnson-1978) | 4.878 | 97.5% Chebyshev (MVUE) UCL | 5.816 |
| | | 99% Chebyshev (MVUE) UCL | 6.485 |

Gamma Distribution Test

| | | | |
|------------------------------------|--------|---|-------|
| k star (bias corrected) | 4.798 | Data Distribution | |
| Theta Star | 0.963 | Data Follow Appr. Gamma Distribution at 5% Significance Level | |
| MLE of Mean | 4.621 | | |
| MLE of Standard Deviation | 2.11 | | |
| nu star | 1746 | | |
| Approximate Chi Square Value (.05) | 1650 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 4.875 |
| Adjusted Chi Square Value | 1650 | 95% Jackknife UCL | 4.876 |
| | | 95% Standard Bootstrap UCL | 4.875 |

Anderson-Darling Test Statistic

| | | | |
|---|--------|-------------------------------|-------|
| Anderson-Darling Test Statistic | 0.987 | 95% Bootstrap-t UCL | 4.898 |
| Anderson-Darling 5% Critical Value | 0.756 | 95% Hall's Bootstrap UCL | 4.91 |
| Kolmogorov-Smirnov Test Statistic | 0.066 | 95% Percentile Bootstrap UCL | 4.877 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0685 | 95% BCA Bootstrap UCL | 4.892 |
| Data follow Appr. Gamma Distribution at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 5.293 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 5.583 |
| | | 99% Chebyshev(Mean, Sd) UCL | 6.154 |

Assuming Gamma Distribution

| | |
|---------------------------|-------|
| 95% Approximate Gamma UCL | 4.89 |
| 95% Adjusted Gamma UCL | 4.893 |

Potential UCL to Use

Use 95% Approximate Gamma UCL 4.89

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Copper

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 165

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|-------|
| | | Log-transformed Statistics | |
| Minimum | 5.78 | Minimum of Log Data | 1.754 |
| Maximum | 832 | Maximum of Log Data | 6.724 |
| Mean | 134.6 | Mean of log Data | 4.382 |
| Median | 95.55 | SD of log Data | 1.104 |
| SD | 140.4 | | |
| Std. Error of Mean | 10.41 | | |
| Coefficient of Variation | 1.043 | | |
| Skewness | 2.163 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.179 | Lilliefors Test Statistic | 0.0735 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 151.8 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 177.1 |
| 95% Adjusted-CLT UCL (Chen-1995) | 153.5 | 95% Chebyshev (MVUE) UCL | 211.6 |
| 95% Modified-t UCL (Johnson-1978) | 152.1 | 97.5% Chebyshev (MVUE) UCL | 239.8 |
| | | 99% Chebyshev (MVUE) UCL | 295.3 |

Gamma Distribution Test

| | | | |
|--|--------|--|-------|
| k star (bias corrected) | 1.083 | Data Distribution | |
| Theta Star | 124.3 | Data appear Gamma Distributed at 5% Significance Level | |
| MLE of Mean | 134.6 | | |
| MLE of Standard Deviation | 129.3 | | |
| nu star | 394.3 | | |
| Approximate Chi Square Value (.05) | 349.3 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 151.8 |
| Adjusted Chi Square Value | 349 | 95% Jackknife UCL | 151.8 |
| | | 95% Standard Bootstrap UCL | 152.2 |
| Anderson-Darling Test Statistic | 0.599 | 95% Bootstrap-t UCL | 154.3 |
| Anderson-Darling 5% Critical Value | 0.781 | 95% Hall's Bootstrap UCL | 153.8 |
| Kolmogorov-Smirnov Test Statistic | 0.0531 | 95% Percentile Bootstrap UCL | 152.5 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0701 | 95% BCA Bootstrap UCL | 154.9 |
| Data appear Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 180 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 199.6 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 238.2 |
| 95% Approximate Gamma UCL | 152 | | |
| 95% Adjusted Gamma UCL | 152.1 | | |

Potential UCL to Use Use 95% Approximate Gamma UCL 152

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Iron

General Statistics

| | | | |
|------------------------------|-----|---------------------------------|-----|
| Number of Valid Observations | 182 | Number of Distinct Observations | 151 |
|------------------------------|-----|---------------------------------|-----|

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|-------|
| Minimum | 396 | Log-transformed Statistics | |
| Maximum | 33200 | Minimum of Log Data | 5.981 |
| Mean | 10715 | Maximum of Log Data | 10.41 |
| Median | 9965 | Mean of log Data | 9.057 |
| SD | 6132 | SD of log Data | 0.792 |
| Std. Error of Mean | 454.6 | | |
| Coefficient of Variation | 0.572 | | |
| Skewness | 0.759 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.11 | Lilliefors Test Statistic | 0.116 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 11466 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 13196 |
| 95% Adjusted-CLT UCL (Chen-1995) | 11490 | 95% Chebyshev (MVUE) UCL | 15109 |
| 95% Modified-t UCL (Johnson-1978) | 11471 | 97.5% Chebyshev (MVUE) UCL | 16583 |
| | | 99% Chebyshev (MVUE) UCL | 19478 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 2.361 | Data Distribution | |
| Theta Star | 4538 | Data do not follow a Discernable Distribution (0.05) | |
| MLE of Mean | 10715 | | |
| MLE of Standard Deviation | 6973 | | |
| nu star | 859.5 | | |
| Approximate Chi Square Value (.05) | 792.5 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 11463 |
| Adjusted Chi Square Value | 792 | 95% Jackknife UCL | 11466 |
| | | 95% Standard Bootstrap UCL | 11465 |
| Anderson-Darling Test Statistic | 2.27 | 95% Bootstrap-t UCL | 11505 |
| Anderson-Darling 5% Critical Value | 0.764 | 95% Hall's Bootstrap UCL | 11508 |
| Kolmogorov-Smirnov Test Statistic | 0.1 | 95% Percentile Bootstrap UCL | 11487 |
| Kolmogorov-Smirnov 5% Critical Value | 0.069 | 95% BCA Bootstrap UCL | 11464 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 12696 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 13554 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 15238 |
| 95% Approximate Gamma UCL | 11621 | | |
| 95% Adjusted Gamma UCL | 11629 | | |

| | | | |
|----------------------|--|----------------------------------|-------|
| Potential UCL to Use | | Use 95% Chebyshev (Mean, Sd) UCL | 12696 |
|----------------------|--|----------------------------------|-------|

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Lead

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 165

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|-------|
| | | Log-transformed Statistics | |
| Minimum | 4.95 | Minimum of Log Data | 1.599 |
| Maximum | 763 | Maximum of Log Data | 6.637 |
| Mean | 131.7 | Mean of log Data | 4.316 |
| Median | 83.7 | SD of log Data | 1.15 |
| SD | 140.5 | | |
| Std. Error of Mean | 10.41 | | |
| Coefficient of Variation | 1.066 | | |
| Skewness | 1.939 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.183 | Lilliefors Test Statistic | 0.0725 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 148.9 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 176.6 |
| 95% Adjusted-CLT UCL (Chen-1995) | 150.5 | 95% Chebyshev (MVUE) UCL | 212.2 |
| 95% Modified-t UCL (Johnson-1978) | 149.2 | 97.5% Chebyshev (MVUE) UCL | 241.6 |
| | | 99% Chebyshev (MVUE) UCL | 299.3 |

Gamma Distribution Test

| | | | |
|---|--------|---|-------|
| k star (bias corrected) | 1.006 | Data Distribution | |
| Theta Star | 131 | Data Follow Appr. Gamma Distribution at 5% Significance Level | |
| MLE of Mean | 131.7 | | |
| MLE of Standard Deviation | 131.3 | | |
| nu star | 366.1 | | |
| Approximate Chi Square Value (.05) | 322.8 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 148.9 |
| Adjusted Chi Square Value | 322.5 | 95% Jackknife UCL | 148.9 |
| | | 95% Standard Bootstrap UCL | 148.8 |
| Anderson-Darling Test Statistic | 0.884 | 95% Bootstrap-t UCL | 151.6 |
| Anderson-Darling 5% Critical Value | 0.783 | 95% Hall's Bootstrap UCL | 151.2 |
| Kolmogorov-Smirnov Test Statistic | 0.0598 | 95% Percentile Bootstrap UCL | 149.3 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0703 | 95% BCA Bootstrap UCL | 150.1 |
| Data follow Appr. Gamma Distribution at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 177.1 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 196.7 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 235.3 |
| 95% Approximate Gamma UCL | 149.4 | | |
| 95% Adjusted Gamma UCL | 149.6 | | |

Potential UCL to Use Use 95% Approximate Gamma UCL 149.4

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Mercury

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 161

Raw Statistics

| | | | |
|--------------------------|---------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.00897 | Minimum of Log Data | -4.714 |
| Maximum | 1.05 | Maximum of Log Data | 0.0488 |
| Mean | 0.104 | Mean of log Data | -2.761 |
| Median | 0.071 | SD of log Data | 1.051 |
| SD | 0.115 | | |
| Std. Error of Mean | 0.00849 | | |
| Coefficient of Variation | 1.105 | | |
| Skewness | 3.79 | | |

Relevant UCL Statistics

| | | | |
|--|--------|--|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.204 | Lilliefors Test Statistic | 0.0654 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 0.118 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 0.131 |
| 95% Adjusted-CLT UCL (Chen-1995) | 0.12 | 95% Chebyshev (MVUE) UCL | 0.155 |
| 95% Modified-t UCL (Johnson-1978) | 0.118 | 97.5% Chebyshev (MVUE) UCL | 0.175 |
| | | 99% Chebyshev (MVUE) UCL | 0.214 |

Gamma Distribution Test

| | | | |
|---|--------|---|-------|
| k star (bias corrected) | 1.136 | Data Distribution | |
| Theta Star | 0.0912 | Data Follow Appr. Gamma Distribution at 5% Significance Level | |
| MLE of Mean | 0.104 | | |
| MLE of Standard Deviation | 0.0972 | | |
| nu star | 413.4 | | |
| Approximate Chi Square Value (.05) | 367.2 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 0.118 |
| Adjusted Chi Square Value | 366.9 | 95% Jackknife UCL | 0.118 |
| | | 95% Standard Bootstrap UCL | 0.118 |
| Anderson-Darling Test Statistic | 0.922 | 95% Bootstrap-t UCL | 0.121 |
| Anderson-Darling 5% Critical Value | 0.78 | 95% Hall's Bootstrap UCL | 0.123 |
| Kolmogorov-Smirnov Test Statistic | 0.0622 | 95% Percentile Bootstrap UCL | 0.118 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0701 | 95% BCA Bootstrap UCL | 0.121 |
| Data follow Appr. Gamma Distribution at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 0.141 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 0.157 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 0.188 |
| 95% Approximate Gamma UCL | 0.117 | | |
| 95% Adjusted Gamma UCL | 0.117 | | |

Potential UCL to Use Use 95% Approximate Gamma UCL 0.117

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Molybdenium

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 160

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.307 | Minimum of Log Data | -1.181 |
| Maximum | 21.8 | Maximum of Log Data | 3.082 |
| Mean | 2.847 | Mean of log Data | 0.597 |
| Median | 1.645 | SD of log Data | 0.924 |
| SD | 3.345 | | |
| Std. Error of Mean | 0.248 | | |
| Coefficient of Variation | 1.175 | | |
| Skewness | 3.168 | | |

Relevant UCL Statistics

| | | | |
|--|--------|--|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.224 | Lilliefors Test Statistic | 0.0607 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 3.257 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 3.218 |
| 95% Adjusted-CLT UCL (Chen-1995) | 3.317 | 95% Chebyshev (MVUE) UCL | 3.755 |
| 95% Modified-t UCL (Johnson-1978) | 3.266 | 97.5% Chebyshev (MVUE) UCL | 4.179 |
| | | 99% Chebyshev (MVUE) UCL | 5.012 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 1.238 | Data Distribution | |
| Theta Star | 2.3 | Data appear Lognormal at 5% Significance Level | |
| MLE of Mean | 2.847 | | |
| MLE of Standard Deviation | 2.559 | | |
| nu star | 450.5 | | |
| Approximate Chi Square Value (.05) | 402.2 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 3.255 |
| Adjusted Chi Square Value | 401.9 | 95% Jackknife UCL | 3.257 |
| | | 95% Standard Bootstrap UCL | 3.265 |
| Anderson-Darling Test Statistic | 3.198 | 95% Bootstrap-t UCL | 3.361 |
| Anderson-Darling 5% Critical Value | 0.777 | 95% Hall's Bootstrap UCL | 3.348 |
| Kolmogorov-Smirnov Test Statistic | 0.106 | 95% Percentile Bootstrap UCL | 3.282 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0699 | 95% BCA Bootstrap UCL | 3.301 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 3.928 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 4.395 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 5.314 |
| 95% Approximate Gamma UCL | 3.188 | | |
| 95% Adjusted Gamma UCL | 3.191 | | |

Potential UCL to Use Use 95% H-UCL 3.218

ProUCL computes and outputs H-statistic based UCLs for historical reasons only. H-statistic often results in unstable (both high and low) values of UCL95 as shown in examples in the Technical Guide. It is therefore recommended to avoid the use of H-statistic based 95% UCLs. Use of nonparametric methods are preferred to compute UCL95 for skewed data sets which do not follow a gamma distribution.

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Nickel

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 164

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.783 | Minimum of Log Data | -0.245 |
| Maximum | 37.4 | Maximum of Log Data | 3.622 |
| Mean | 6.046 | Mean of log Data | 1.645 |
| Median | 5.455 | SD of log Data | 0.545 |
| SD | 4.427 | | |
| Std. Error of Mean | 0.328 | | |
| Coefficient of Variation | 0.732 | | |
| Skewness | 4.563 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.227 | Lilliefors Test Statistic | 0.109 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 6.589 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 6.474 |
| 95% Adjusted-CLT UCL (Chen-1995) | 6.704 | 95% Chebyshev (MVUE) UCL | 7.133 |
| 95% Modified-t UCL (Johnson-1978) | 6.607 | 97.5% Chebyshev (MVUE) UCL | 7.621 |
| | | 99% Chebyshev (MVUE) UCL | 8.58 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 3.343 | Data Distribution | |
| Theta Star | 1.808 | Data do not follow a Discernable Distribution (0.05) | |
| MLE of Mean | 6.046 | | |
| MLE of Standard Deviation | 3.307 | | |
| nu star | 1217 | | |
| Approximate Chi Square Value (.05) | 1137 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 6.586 |
| Adjusted Chi Square Value | 1136 | 95% Jackknife UCL | 6.589 |
| | | 95% Standard Bootstrap UCL | 6.595 |
| Anderson-Darling Test Statistic | 5.109 | 95% Bootstrap-t UCL | 6.837 |
| Anderson-Darling 5% Critical Value | 0.759 | 95% Hall's Bootstrap UCL | 6.895 |
| Kolmogorov-Smirnov Test Statistic | 0.138 | 95% Percentile Bootstrap UCL | 6.648 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0687 | 95% BCA Bootstrap UCL | 6.73 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 7.476 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 8.095 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 9.311 |
| 95% Approximate Gamma UCL | 6.471 | | |
| 95% Adjusted Gamma UCL | 6.475 | | |

Potential UCL to Use Use 95% Chebyshev (Mean, Sd) UCL 7.476

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Selenium

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 154

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.144 | Minimum of Log Data | -1.938 |
| Maximum | 23 | Maximum of Log Data | 3.135 |
| Mean | 2.007 | Mean of log Data | 0.0989 |
| Median | 1.16 | SD of log Data | 1.009 |
| SD | 3.345 | | |
| Std. Error of Mean | 0.248 | | |
| Coefficient of Variation | 1.666 | | |
| Skewness | 4.193 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.306 | Lilliefors Test Statistic | 0.0775 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 2.417 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 2.163 |
| 95% Adjusted-CLT UCL (Chen-1995) | 2.497 | 95% Chebyshev (MVUE) UCL | 2.554 |
| 95% Modified-t UCL (Johnson-1978) | 2.43 | 97.5% Chebyshev (MVUE) UCL | 2.867 |
| | | 99% Chebyshev (MVUE) UCL | 3.483 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 0.957 | Data Distribution | |
| Theta Star | 2.098 | Data do not follow a Discernable Distribution (0.05) | |
| MLE of Mean | 2.007 | | |
| MLE of Standard Deviation | 2.052 | | |
| nu star | 348.2 | | |
| Approximate Chi Square Value (.05) | 306 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 2.415 |
| Adjusted Chi Square Value | 305.7 | 95% Jackknife UCL | 2.417 |
| | | 95% Standard Bootstrap UCL | 2.416 |
| Anderson-Darling Test Statistic | 7.486 | 95% Bootstrap-t UCL | 2.557 |
| Anderson-Darling 5% Critical Value | 0.785 | 95% Hall's Bootstrap UCL | 2.501 |
| Kolmogorov-Smirnov Test Statistic | 0.168 | 95% Percentile Bootstrap UCL | 2.461 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0704 | 95% BCA Bootstrap UCL | 2.489 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 3.088 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 3.556 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 4.474 |
| 95% Approximate Gamma UCL | 2.284 | | |
| 95% Adjusted Gamma UCL | 2.287 | | |

Potential UCL to Use Use 95% Chebyshev (Mean, Sd) UCL 3.088

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Silver

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 148

Raw Statistics

| | | | |
|--------------------------|--------|----------------------------|--------|
| | | Log-transformed Statistics | |
| Minimum | 0.0816 | Minimum of Log Data | -2.506 |
| Maximum | 3.14 | Maximum of Log Data | 1.144 |
| Mean | 0.464 | Mean of log Data | -1.311 |
| Median | 0.194 | SD of log Data | 1.01 |
| SD | 0.543 | | |
| Std. Error of Mean | 0.0402 | | |
| Coefficient of Variation | 1.168 | | |
| Skewness | 2.171 | | |

Relevant UCL Statistics

| | | | |
|--|--------|---|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.24 | Lilliefors Test Statistic | 0.181 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data not Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 0.531 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 0.529 |
| 95% Adjusted-CLT UCL (Chen-1995) | 0.537 | 95% Chebyshev (MVUE) UCL | 0.625 |
| 95% Modified-t UCL (Johnson-1978) | 0.532 | 97.5% Chebyshev (MVUE) UCL | 0.701 |
| | | 99% Chebyshev (MVUE) UCL | 0.852 |

Gamma Distribution Test

| | | | |
|---|--------|--|-------|
| k star (bias corrected) | 1.042 | Data Distribution | |
| Theta Star | 0.446 | Data do not follow a Discernable Distribution (0.05) | |
| MLE of Mean | 0.464 | | |
| MLE of Standard Deviation | 0.455 | | |
| nu star | 379.2 | | |
| Approximate Chi Square Value (.05) | 335.1 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 0.53 |
| Adjusted Chi Square Value | 334.8 | 95% Jackknife UCL | 0.531 |
| | | 95% Standard Bootstrap UCL | 0.53 |
| Anderson-Darling Test Statistic | 10.06 | 95% Bootstrap-t UCL | 0.543 |
| Anderson-Darling 5% Critical Value | 0.782 | 95% Hall's Bootstrap UCL | 0.537 |
| Kolmogorov-Smirnov Test Statistic | 0.185 | 95% Percentile Bootstrap UCL | 0.534 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0702 | 95% BCA Bootstrap UCL | 0.532 |
| Data not Gamma Distributed at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 0.64 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 0.715 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 0.864 |
| 95% Approximate Gamma UCL | 0.525 | | |
| 95% Adjusted Gamma UCL | 0.526 | | |

Potential UCL to Use Use 95% Chebyshev (Mean, Sd) UCL 0.64

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.

Zinc

General Statistics

Number of Valid Observations 182 Number of Distinct Observations 157

Raw Statistics

| | | | |
|--------------------------|-------|----------------------------|-------|
| | | Log-transformed Statistics | |
| Minimum | 8.16 | Minimum of Log Data | 2.099 |
| Maximum | 617 | Maximum of Log Data | 6.425 |
| Mean | 138.3 | Mean of log Data | 4.611 |
| Median | 110 | SD of log Data | 0.832 |
| SD | 113 | | |
| Std. Error of Mean | 8.375 | | |
| Coefficient of Variation | 0.817 | | |
| Skewness | 1.561 | | |

Relevant UCL Statistics

| | | | |
|--|--------|--|--------|
| Normal Distribution Test | | Lognormal Distribution Test | |
| Lilliefors Test Statistic | 0.146 | Lilliefors Test Statistic | 0.0515 |
| Lilliefors Critical Value | 0.0657 | Lilliefors Critical Value | 0.0657 |
| Data not Normal at 5% Significance Level | | Data appear Lognormal at 5% Significance Level | |

Assuming Normal Distribution

| | | | |
|-----------------------------------|-------|---------------------------------|-------|
| 95% Student's-t UCL | 152.1 | Assuming Lognormal Distribution | |
| 95% UCLs (Adjusted for Skewness) | | 95% H-UCL | 161.3 |
| 95% Adjusted-CLT UCL (Chen-1995) | 153.1 | 95% Chebyshev (MVUE) UCL | 185.8 |
| 95% Modified-t UCL (Johnson-1978) | 152.3 | 97.5% Chebyshev (MVUE) UCL | 204.8 |
| | | 99% Chebyshev (MVUE) UCL | 242.1 |

Gamma Distribution Test

| | | | |
|---|--------|---|-------|
| k star (bias corrected) | 1.693 | Data Distribution | |
| Theta Star | 81.67 | Data Follow Appr. Gamma Distribution at 5% Significance Level | |
| MLE of Mean | 138.3 | | |
| MLE of Standard Deviation | 106.3 | | |
| nu star | 616.4 | | |
| Approximate Chi Square Value (.05) | 559.8 | Nonparametric Statistics | |
| Adjusted Level of Significance | 0.0487 | 95% CLT UCL | 152.1 |
| Adjusted Chi Square Value | 559.4 | 95% Jackknife UCL | 152.1 |
| | | 95% Standard Bootstrap UCL | 152.1 |
| Anderson-Darling Test Statistic | 0.794 | 95% Bootstrap-t UCL | 153.3 |
| Anderson-Darling 5% Critical Value | 0.769 | 95% Hall's Bootstrap UCL | 153.2 |
| Kolmogorov-Smirnov Test Statistic | 0.0633 | 95% Percentile Bootstrap UCL | 151.9 |
| Kolmogorov-Smirnov 5% Critical Value | 0.0694 | 95% BCA Bootstrap UCL | 153.4 |
| Data follow Appr. Gamma Distribution at 5% Significance Level | | 95% Chebyshev(Mean, Sd) UCL | 174.8 |
| | | 97.5% Chebyshev(Mean, Sd) UCL | 190.6 |
| Assuming Gamma Distribution | | 99% Chebyshev(Mean, Sd) UCL | 221.6 |

| | |
|---------------------------|-------|
| 95% Approximate Gamma UCL | 152.3 |
| 95% Adjusted Gamma UCL | 152.4 |

Potential UCL to Use Use 95% Approximate Gamma UCL 152.3

Note: Suggestions regarding the selection of a 95% UCL are provided to help the user to select the most appropriate 95% UCL. These recommendations are based upon the results of the simulation studies summarized in Singh, Singh, and Iaci (2002) and Singh and Singh (2003). For additional insight, the user may want to consult a statistician.